

## Mark schemes

## Q1.

(a)  $\lambda = 2 \times 0.648$

*Allow 1296 (mm) or 1.296 (m) or 129.6 (cm) seen.***OR**Use of  $v = f \lambda$  ✓*Condone **one error** in their substitution where  $\lambda$  and  $f$  have been substituted and  $v$  would be the subject:**Allow*

*(v=)  $0.648 \times 147$  (forgets to double  $L$ )*

*OR*

*(v=)  $\frac{0.648}{2} \times 147$  (halves  $L$ )*

*Do not allow:*

*(v=)  $648 \times 147$  (POT error **and** forgets to double  $L$ )*

*NOR*

*(v=)  $\frac{648}{2} \times 147$  (POT error **and** halves  $L$ )*

$(v =) 191 \text{ (m s}^{-1}\text{)} \checkmark$

*Calculator display= 190.512**190 (ms<sup>-1</sup>) correct to 2 sf*

2

(b) Use of  $f = \frac{1}{2l} \sqrt{\frac{T}{\mu}}$

**OR**

Use of  $v = \sqrt{\frac{T}{\mu}}$

**OR***Condone **one error** where  $f$ ,  $l$  and  $T$  have been substituted.**OR* *$\mu$  would be subject of a correctly rearranged*

*expression  $(\mu =) \frac{T}{4l^2 f^2}$*

$(\mu =) 1.956 \times 10^{-3} \text{ (kg m}^{-1}\text{)} \checkmark$

*Their  $l$ :**must be seen in **MP1**:****or****condone a POT error (if already penalised in **MP1** or part (a))*

Use of

$m = \text{their } \mu \times \text{their } l \checkmark$

allow ecf from part (a) where  $v = \sqrt{\frac{T}{\mu}}$  seen

**MP1**  $\mu = \frac{T}{v^2}$  or  $\mu = 71$  / answer to part (a)

**MP2** ( $m =$ ) their ecf  $\mu \times 0.648$

**MP3 ecf answer**

( $m =$ )  $1.3 \times 10^{-3}$  (kg)  $\checkmark$

Calculator display =  $1.267618831 \times 10^{-3}$  (kg)

3

[5]

## Q2.

(a) between  $s = 7.5$  m and  $s = 15$  m  $\checkmark$

Tick in 2nd box only

1

(b) Use of  $\Delta E_P = mgh \checkmark$

Use of: rearrangement where  $m$  would be subject or substitution.

Condone **one error** in substitution.

( $m =$ )  $65(.0)$  (kg)  $\checkmark$

Calculator display =

For  $g = 9.81 \text{ ms}^{-2} = 64.96772001$

For  $g = 9.8 \text{ ms}^{-2} = 65.0340136054421$

Alternative method for an ECF from **part (a)** (tick in 3<sup>rd</sup> or 4<sup>th</sup> boxes).

• Use of  $E_k = \frac{1}{2}mv^2$

**OR**

Read-off for  $v = 15.4 \text{ ms}^{-1}$  (Acceptable range  $15.2 \text{ ms}^{-1}$  to  $15.6 \text{ ms}^{-1}$ )

•  $m = 80.6$  (kg)

(Acceptable range  $78.57 \text{ kg}$  to  $82.76 \text{ kg}$ )

2

(c) Max 2 from: ✓✓

- Energy difference ( $E$ ) =  $9.56 - 7.71 = 1.85$  (kJ) ✓  
Accept correct energy conservation statement for **MP1**

For example:

$$\Delta E_P = E_K + \text{energy stored (in rope)}$$

- Use of  $E = \frac{1}{2}k\Delta L^2$

Use of:

Rearrangement to make  $\Delta L$  the subject or by substitution.Condone use of their  $E$  and **one other error** in substitution. (allow 9.56 (kJ) or 7.71(kJ) for  $E$ )

Condone use of

$$E = \frac{1}{2}F\Delta L \quad \text{and } F = k\Delta L \quad \text{OR}$$

$$E = \frac{1}{2}F\Delta L \quad \text{and } F = mg$$

With their  $F$  and their  $E$  seen in  $E = \frac{1}{2}F\Delta L$ 

- $$\Delta L = \sqrt{\frac{2 \times \text{their energy difference}}{k}}$$

Must be an energy difference. Condone POT

Do not accept 9.56 (kJ) or 7.71(kJ) for their energy difference.

$$\Delta L = 5.8(0) \text{ m } \checkmark$$

Max 1 mark for:

$$637.65 = 110 \times \Delta L \text{ giving } \Delta L = 5.8 \text{ m}$$

must be done by considering energy transfers.

**OR**

answer without working.

**[6]**

**Q3.**

- (a) calculates, using all 4 values, a mean of 0.418 (s) ✓  
*Expect to see 25.08 (mean average) divided by 60,  
 or 100.32 (sum) divided by 240 in working*

1

- (b) 2.75 cycles (between **P** and **Q**) <sub>1</sub>✓

$$T_{PQ} = 0.42 \times \text{their number of cycles} \text{ } _2\checkmark$$

*Expect  $T_{PQ} = 1.15, 1.16$  or  $1.2$  (s)*

<sub>2</sub>✓ Allow use of >2 sf  $T_{PQ}$  that rounds to 0.42 (s)

<sub>2</sub>✓ Their number of cycles must be between 2.5 and 3

2

- (c) 0.170 (m) ✓

*Condone 2 sf value on answer line if working shows  
 a 3 sf value or "170 mm" seen or "20 mm" used e.g.  
 '8.5 × 20 mm'.*

1

- (d) correct use of an appropriate equation of motion <sub>1</sub>✓

correct evaluation of their  $a$  <sub>2</sub>✓

*Expect to see  $a = 0.24, 0.25$  or  $0.26$  ( $m s^{-2}$ )*

$$_1\checkmark \text{ Expect } a = \frac{2 \times \text{their } s}{\text{their } (T_{PQ})^2} \text{ OR}$$

$$\text{mean } v = \frac{\text{their } s}{\text{their } T_{PQ}} \text{ AND } a = \frac{2 \times \text{their mean } v}{\text{their } T_{PQ}}$$

*Expect mean  $v = 0.14$  or  $0.15$  ( $m s^{-1}$ )*

<sub>1</sub>✓ Allow  $s$  in mm

2

**[6]**

**Q4.**

- (a) value in range  $2.9 \times 10^4$  to  $3.0 \times 10^4$  (N) ✓

*Use of data from any point (plotted or using their line or using their B for brass) is acceptable*

1

- (b) smooth curve through at least 4 saltires <sub>1a</sub>✓

<sub>1a</sub>✓ *Reject thick or discontinuous lines*

<sub>1a</sub>✓ *can be awarded if no credit gained in* <sub>1b</sub>✓ *or* <sub>2b</sub>✓

correct read off at 1.60 mm, leading to answer in range 58 to 64 ( $\text{kg mm}^{-2}$ )

<sub>2a</sub>✓

<sub>2a</sub>✓ *2 or 3 sf values only*

**OR**

use of  $B = \frac{\text{their } F}{\pi \times g \times 10 \times 1.6}$  <sub>1b</sub>✓

<sub>1b</sub>✓ *Condone use of D and h in metres if also seen (and penalised) in **part (a)***

consistent calculation of B <sub>2b</sub>✓

<sub>2b</sub>✓ *2 or 3 sf values only*

<sub>2b</sub>✓ *Their B should be*  $\frac{\text{their } F}{493}$

2

**[3]**

**Q5.**

- (a) use of  $\rho = \frac{m}{V}$  AND  $V = Al$   $_1\checkmark$

260 (m)  $_2\checkmark$

$_1\checkmark$  Expect to see  $V = 2.5 \text{ m}^3$  or total  $V = 5.0 \text{ m}^3$

2

- (b) calculates total tension of  $3.2 \times 10^6 \text{ N}$   $_1\checkmark$

$F = T - W$  seen **OR** subtracts a weight from tension  $_2\checkmark$

uses  $F = ma$   $_3\checkmark$

0.28 or 0.29 ( $\text{m s}^{-2}$ )  $_4\checkmark$

*Expected values seen:*

*Total mass =  $3.17 \times 10^5 \text{ kg}$*

*Load weight =  $2.75 \times 10^6 \text{ N}$*

*Cable weight =  $3.63 \times 10^5 \text{ N}$*

*Total weight =  $3.11 \times 10^6 \text{ N}$*

*Resultant force =  $9.02 \times 10^4 \text{ N}$*

$_4\checkmark$  Calculator values are: 0.28464 (using  $g = 9.81$ )  
and 0.29464 (using  $g = 9.8$ )

4

**[6]****Q6.**

- (a)  $n = 43.1 \checkmark$  ( $\geq 2$  SF)

$$n = \frac{105 \times 10^3 \times 1}{8.31 \times (273 + 20.0)}$$

1

- (b) Use of  $m = \frac{\rho V}{nN_A}$  OR  $m = \rho V$

OR use of  $m_{\text{molecule}} = \frac{m_{\text{gas}}}{N_A}$  OR  $N = nN_A$

OR  $(c_{\text{rms}})^2 = \frac{3p}{\rho}$  seen in any form

OR use of their mass with  $pV = \frac{1}{3}Nm(c_{\text{rms}})^2$

OR use of  $\frac{1}{2}m(c_{\text{rms}})^2 = \frac{3}{2}kT \checkmark_1$

Correct answer see table  $\checkmark_2$

Correct SF see table  $\checkmark_3$ 

| <b>n</b>                                                      | <b><math>\checkmark_2</math><br/><math>c_{\text{rms}}/\text{m s}^{-1}</math></b> | <b><math>\checkmark_3</math><br/><b>SF</b></b> |
|---------------------------------------------------------------|----------------------------------------------------------------------------------|------------------------------------------------|
| Without $n$                                                   | 500-503                                                                          | 3 SF<br>(501-503)                              |
| $n$ more than 3SF                                             | 500-503                                                                          | 3 SF<br>(501-503)                              |
| 43.1                                                          | 500-503                                                                          | 3 SF<br>(501-503)                              |
| 43                                                            | 500-503                                                                          | 2 SF (500)                                     |
| 40<br>(no evidence<br>of $n = 43$ in<br><b>part (a)</b> )     | 482-484 or<br>500                                                                | 2 or 1 SF (480<br>or 500)                      |
| 40<br>(evidence of $n$<br>$= 43$ in part<br><b>part (a)</b> ) | 482-484 or<br>500                                                                | 1 SF (500)                                     |

*Allow ecf for incorrect  $T$  and/or  $n$  in part (a)**Several approaches are possible*

$$m = \frac{pV}{nN_A} = \frac{1.25 \times 1.00}{43.1 \times 6.02 \times 10^{23}} = 4.82 \times 10^{-26}$$

*(5.1  $\times 10^{-26}$  if 40 used)*

$$c_{\text{rms}} = \sqrt{\frac{3kT}{m}} = \sqrt{\frac{3 \times 1.38 \times 10^{-23} \times 293}{4.82 \times 10^{-26}}} = 502$$

OR

$$pV = \frac{1}{3}Nm(c_{\text{rms}})^2 \quad p \frac{Nm}{\rho} = \frac{1}{3}Nm(c_{\text{rms}})^2$$

$$(c_{\text{rms}})^2 = \frac{3p}{\rho} \left( = \frac{3pV}{Nm} = \frac{3p \times 1}{\rho} \right)$$

$$c_{\text{rms}} = \sqrt{\frac{3 \times 105 \times 10^3}{1.25}} = 502$$

- (c)  $T = 4 \times 293$  or 4 times the starting temperature in K ✓

change in temperature = 879 (K) ✓ (correct answer gains both marks)

### Alternative

$$T = \frac{m(2c_{\text{rms}})^2}{3k} \text{ correctly calculated for their } m, c_{\text{rms}} \checkmark$$

Their calculated  $T$  - 293 ✓ 7709

$$\text{mp1 Using } \frac{1}{2}m(c_{\text{rms}})^2 = \frac{3}{2}kT \text{ so } (c_{\text{rms}})^2 \propto T$$

$$\frac{(c_{\text{rms}})^2}{293} = \frac{(2 \times c_{\text{rms}})^2}{T}$$

$$T = 293 \times 4 = 1172 \text{ K}$$

$$\text{mp2 change in temperature} = 1172 - 293 = 879 \text{ K}$$

Allow answer that rounds to 880 (K)

If no other marks awarded award max 1 when  $T$  is 4 times original and  $\Delta\theta = 60$

2

- (d) Max 2 from: ✓✓

- Calculation of mass of water condensed in one hour  $1.25 \times 960 \times (0.0057 - 0.0037) = 2.4 \text{ (kg)}$
- use of their mass with  $mc\Delta\theta$  (expect  $4.5 \times 10^4 \text{ (J)}$ )
- use of their mass with  $mL$  (expect  $5.5(2) \times 10^6 \text{ (J)}$ )

heat energy removed =  $5.6 \times 10^6 \text{ (J)}$  ✓

3

[9]

## Q7.

(a) Max 2 ✓✓

$$\omega = \frac{2\pi}{T} = \frac{2\pi}{27.3 \times 24 \times 60 \times 60} = 2.664 \times 10^{-6} \text{ (rad s}^{-1}\text{)}$$

$$\text{or } v = \frac{2\pi r}{T} = \frac{2\pi \times 4.489 \times 10^8}{27.3 \times 24 \times 60 \times 60} = 1196 \text{ (m s}^{-1}\text{)}$$

Substitution or value

- Idea (resultant) gravitational field strength is equal to centripetal acceleration e.g.

$$g_R = a \text{ or } g_R = rw^2 \text{ or } g_R = \frac{v^2}{r} (= 3.19 \times 10^{-3} \text{ m s}^{-2})$$

- Idea that  $g_M = g_R - g_E$

*MP1 may be part of MP2**Ignore PoT, rounding errors and minor copy errors for MP1 and MP2**A substitution into  $T^2 = \frac{4\pi^2 r^3}{GM}$  or equivalent is not accepted for the first bullet.**In the second bullet point do not allow  $g_m$* *MP3 must follow from correct working*

$$1.21 \times 10^{-3} \geq 3 \text{ SF from correct working } \checkmark \text{ (N kg}^{-1}\text{)}$$

3

(b)

$$r = \sqrt{\frac{GM}{g_M}} = \sqrt{\frac{6.67 \times 10^{-11} \times 7.35 \times 10^{22}}{1.21 \times 10^{-3}}} \checkmark$$

*Allow ecf from **part (a)***

$$6.37 \times 10^7 \text{ (m)} \checkmark$$

*Allow  $6.38 \times 10^7$  or  $6.39 \times 10^7$  or  $6.4 \times 10^7$  (m)*

2

**[5]**

**Q8.**

- (a) Determination of focal length of objective

OR adds their  $f_o$  and  $f_e$  ✓

$$f_o = M \times f_e = 75 \times 0.022 = 1.65 \text{ (m)}$$

1.67 (m) CAO ✓

*No sf penalty*

*Condone 2 sf 1.7*

2

- (b) Determination of angle subtended by Jupiter at unaided eye

OR uses:

distance to Jupiter = diameter of Jupiter ÷ angle subtended with their diameter OR their angle ✓

*E.g.*

$$1.7 \times 10^{-2} / 75 = 2.3 \times 10^{-4} \text{ (rad)}$$

$$2 \times 7.0 \times 10^4 / 2.3 \times 10^{-4}$$

*In MP1 allow use of trig and angle in degrees or radians. Condone use of  $1.7 \times 10^{-2}$  degrees.*

distance =  $6.2 \times 10^8$  (km) ✓ CAO

*Do not award MP1 if both angle and diameter are incorrect.*

2

**[4]**

**Q9.**

- (a) Determines  $s$  and  $r$  in consistent units  
OR

Uses  $A = 2 \times \text{parallax angle} = 2 \times (1 \div \frac{79}{3.26})$

✓

eg for MP1

- $s = 2 \times 1.5 \times 10^{11} \text{ m}; r = 79 \times 9.46 \times 10^{15} \text{ m}$
- $s = 2 \div 2.06 \times 10^5 \text{ pc}; r = 79 \div 3.26 \text{ pc}$
- $\tan(A/2) = \text{orbital radius} \div \text{distance to star}$   
with consistent units

$$A = 4.0 \times 10^{-7} \text{ rad} = 2.3 \times 10^{-5} \text{ degrees}$$

Evidence for MP1 can be seen in the figure.

$2.3 \times 10^{-5}$  degrees CAO ✓

2

- (b) Use of  $m - M = 5 \log(d/10)$  with two correctly substituted from  $m$ ,  $M$  or  $d$   
1✓

*If no other mark given, award 1 mark for recognition that 0.40 pc is a lot less than the distance to nearest known star and therefore determination must be incorrect.*

*For MP2 expect to see*

Obtains correct value of  $m$ ,  $M$  or  $d$  2✓

$$d = 2.3 \text{ pc OR } m = 9.7 \text{ OR } M = 20.5$$

*Alternative for MP1 and MP2*

*using  $m$ ,  $M$  and  $d$  in  $m - M = 5 \log(d/10)$  1✓*

*seeing -3.2 for LHS and -7.0 for RHS 2✓*

Compares **their** value with value given in question 3✓

*MP3 and MP4 cannot be awarded without a comparison of the distances.*

Makes comment about significance of difference between **their** values related to the distance AND some idea of whether the astronomer's suggestion is valid consistent with their values. 4✓

*MP4 is for a recognition of the large difference between their calculated value and value given in question eg by proportion, >>, 6 x bigger, significantly bigger etc.*

*If a difference is calculated in MP3, for MP4 to be awarded the difference must be compared to one of the distances.*

4

[6]

**Q10.**

- (a) Use of  $\lambda_{\max} T = \text{constant}$  to determine their  $\lambda_{\max}$ , their  $T$  or their constant ✓

*Throughout the answer:*

*Allow 0.47 to 0.49  $\mu\text{m}$  for  $\lambda_{\max}$  from the graph*

Comparison with  $\lambda_{\max} = 0.48 \times 10^{-6} \text{ (m)}$  OR  $T = 6.0(4) \times 10^3 \text{ (K)}$  OR constant = 0.0029 m K

AND conclusion that the graph is consistent. ✓

*Allow  $6.17 \times 10^3$  to  $5.92 \times 10^3 \text{ (K)}$  for their calculated  $T$ .*

*Allow  $2.82 \times 10^{-3}$  to  $2.94 \times 10^{-3} \text{ (m K)}$  for their calculated constant.*

2

- (b) Using  $P = \sigma AT^4$  to give

$$P = 5.67 \times 10^{-8} \times 4\pi \times (9.6 \times 10^6)^2 \times 6000^4 \quad \checkmark$$

*In MP1 condone **one** error from*

- *missing the 4*
- *missing the  $\pi$*
- *doubling the radius and using it as  $r$  in an area calculation*
- *POT errors*

*Condone  $\sigma$  for  $5.67 \times 10^{-8}$*

$$8.5 \times 10^{22} \text{ (W)} \quad \checkmark$$

*Allow full credit for use of their  $T$  from **part (a)***

*eg  $T = 6.04 \times 10^3 \text{ (K)}$  gives  $8.75 \times 10^{22} \text{ (W)}$*

2

**[4]**

**Q11.**

- (a) Idea that Hubble's Law is used to estimate the age of the Universe. ✓

*Allow determination of  $H^{-1}$  or  $H$  for the values in the question.*

*Accept idea that age is related to gradient of graph of  $v$  against  $d$ .*

So no, as Andromeda is approaching / is blue-shifted ✓

*Allow “;Hubble's Law is only used with receding/redshifted galaxies.”*

2

- (b) Calculates mass of black hole =  $1.60 \times 10^8 \times 1.99 \times 10^{30}$  ✓

*Correct answer gets  $1\sqrt{2}\checkmark$*

*Correct answer with correct unit gets  $1\sqrt{2}\checkmark_3\checkmark$*

Use of

$$R_s = \frac{2 \times 6.67 \times 10^{-11} \times \text{their mass of black hole}}{(3 \times 10^8)^2} \quad 2\checkmark$$

$$= 4.7 \times 10^{11} \text{ m} \quad 3\checkmark$$

*Also accept*

$$4.7 \times 10^8 \text{ km}$$

$$3.1 \text{ AU}$$

$$1.5 \times 10^{-5} \text{ pc}$$

$$5.0 \times 10^{-5} \text{ ly}$$

*Unit mark is based on correct calculation.*

3

**[5]**

**Q12.**

(a) MAX 4 from:

- Attempts to find area of large loop
- Subtracts area of small loop
- Shows suitable scaling factor
- Uses 4 cycles  $s^{-1}$
- correctly calculates indicated power using their values.

592 W ✓ (cao)

*eg counting small squares*

*157 - 9 squares = 148 squares*

*scaling factor of  $0.10 \times 10^{-3} \times 0.1 \times 10^5 = 1.0 \text{ J per square}$*

*148 J  $\times 1.0 = 148 \text{ J}$*

*If counting 'large' squares:*

*(6.5 - 0.5) squares  $\times 0.50 \times 10^{-3} \times 0.50 \times 10^5$*

*gives 150 J*

*Accept approximating to triangles*

*cycles  $s^{-1} = 4$  (as it is double acting at 2 rev  $s^{-1}$ )*

*indicated power =  $148 \times 4 = 592 \text{ W} \pm 30 \text{ W}$*

5

(b) Input power =  $6.44 \times 10^{-4} \times 18.0 \times 10^6 = 11.6 \times 10^3 \text{ W}$  ✓

Output power =  $T\omega = 39.0 \times 2 \times 2\pi = 490 \text{ W}$  ✓

*Correct answers only*

*Accept  $1.2 \times 10^4 \text{ W}$  or 12000W*

*Condone working not shown provided answers are correct.*

2

[7]

**Q13.**

- (a) Either conversion of 1 MeV to J or
- $W = QV$

$$1.60 \times 10^{-19} \times 1.30 \times 10^6 = 2.08 \times 10^{-13} \checkmark \text{ (J)}$$

*At least 2 sf required.*

1

- (b)
- $Q = mc\Delta\theta = 1.5 \times 903 \times 68.0 (= 92\,106 \text{ J})$
- OR**

$$E_K \text{ of one electron} = \frac{92\,106}{4.50 \times 10^{17}} \checkmark (= 2.05 \times 10^{-13} \text{ J})$$

Both calculations and correct conclusion, eg

Yes, this is consistent with an accelerating voltage of 1.30 MV.  $\checkmark$

*Alternative route*

*Total  $E_K$  for all electrons =*

$$2.08 \times 10^{-13} \times 4.50 \times 10^{17} = (93\,600 \text{ J}) \text{ **OR**}$$

$$\Delta\theta = \frac{Q}{mc} = \frac{93\,600}{1.5 \times 903} \checkmark (= 69.1 \text{ K})$$

*which is consistent with the temperature rise observed.  $\checkmark$*

*Can also compare total  $E_K$  with  $mc\Delta\theta$  for MP2.*

*Use of  $2.0 \times 10^{-13}$  gives total  $E_K$  of 90 000 J and  $\Delta\theta$  of 66 K which is consistent.*

*Allow comparison of in eV or accelerating pd ( $1.28 \times 10^6$ ) with  $1.3 \times 10^6$  V or MeV with MV.*

2

- (c) Correct calculation of non-relativistic
- $E_K$
- $\checkmark_a$

Statement or attempted use of  $E_K = mc^2 - m_0c^2$   $\checkmark_b$

Correct calculation of relativistic  $E_K$   $\checkmark_c$

Both calculations and comparison of with  $2.1 \times 10^{-13}$  or  $2.0 \times 10^{-13}$  J to conclusion consistent with idea that student B is correct  $\checkmark_d$

$$E_K = \frac{1}{2}mv^2 = 3.78 \times 10^{-14} \text{ J}$$

$$E = \frac{m_0c^2}{\sqrt{1-\frac{v^2}{c^2}}} - m_0c^2 = 2.11 \times 10^{-13} \text{ J}$$

*For  $\checkmark_d$  allow a comparison of  $\Delta\theta$  from*

$$m_Ac\Delta\theta = N(mc^2 - m_0c^2) \text{ with } 68^\circ$$

*Allow ecf for  $\checkmark_d$  for minor calculation error, rounding error or transcription errors but there must be a relativistic KE and non-relativistic calculation to award  $\checkmark_d$ .*

**Alternative**

Calculation of speed using  $v = \sqrt{\frac{2E_k}{m}}$  ✓<sub>a</sub>

Statement or attempted use of  $E_k = mc^2 - m_0c^2$  ✓<sub>b</sub>

Calculation of speed from relativistic equation ✓<sub>c</sub>

Both calculations and comparison of results with  $2.88 \times 10^8$  or  $3 \times 10^8$  ✓<sub>d</sub>

$$v = 6.8 \times 10^8 \text{ m s}^{-1} \text{ if using } 2.08 \times 10^{-13}$$

$$v = 2.88 \times 10^8 \text{ m s}^{-1} \text{ if using } 2.08 \times 10^{-13}$$

*Allow calculations based on the total number of electrons and comparison with **part (b)**.*

**Alternative** for Max 2

Correct calculation of non-relativistic  $E_k$  ✓<sub>a</sub>

Calculation of relativistic mass, total energy or  $\sqrt{1 - v^2/c^2}$  or  $\frac{1}{\sqrt{1 - v^2/c^2}}$  AND comment that **relativistic effects are significant (owtte)** so B is correct.

✓<sub>bcd</sub>

*If no other marks awarded max 1 for student B is correct because speed is greater than  $3.0 \times 10^7 \text{ m s}^{-1}$  or  $v$  is 96% of  $c$  (which is greater than 10%).*

4

(d) < 29.8 ns ✓

1

[8]

**Q14.**

(a) (Use of volume (per sec) =)  $\frac{\pi d^2}{4} \times 17.2 \checkmark$   
 (Volume per second =)  $19.45 \text{ (m}^3 \text{ s}^{-1}) = \frac{774\pi}{125}$   
 $\frac{\pi d^2}{4} \times 17.2 = \frac{9\pi}{25} \times 17.2$

Use of  $\rho = \frac{m}{V} \checkmark$

*Substitutes their volume (per second) and density where  $\frac{m}{t}$  would be subject. Do not award MP2 if 2 errors are made in substitution.*

(mass per second =)  $0.389 \text{ (kg s}^{-1}) \checkmark$

*Answer seen to at least 2 sf.*

*Calculator display = 0.3890548342*

3

(b) Use of  $F = \frac{m}{t} \times v$  or  $(F =) 6.69 \text{ N}$  or  $6.708 \text{ (N)}$  or  $6.88 \text{ (N)}$

**OR**

Use of  $W=mg$

**OR** statement:

Upward force = weight  $\checkmark$

*Possible ECF from (a) where their m rounds to 0.4 kg.*

*$W = 3.72m$  seen or  $3.72m$  as the subject of a force equation.*

*Do not allow  $3.72 \times 0.4$  as use of  $W=mg$*

Applies condition for equilibrium by setting  $F = mg$

**OR**

$6.69 = 3.72 m$  or  $6.708 = 3.72 m$  or  $6.88 = 3.72 m \checkmark$

$(m =) 1.80 \text{ (kg)} \checkmark$

*Accept answer correctly rounded to at least 2 sf.*

$F = 6.88 \text{ N}$  where  $\frac{m}{t} = 0.4$

$m = 1.85 \text{ kg}$  or  $1.8 \text{ kg}$

3

(c) Use of  $E = Pt$ 

OR

converts kWh to J ✓

$$(E =) 340 \times 39 \text{ or } 13260 \text{ (J)}$$

$$(0.035 \text{ kWh} =) 35 \times 3600 \text{ or } 126000 \text{ (J)}$$

**Alternative MP1** converts to any of the following units of energy.

$$\bullet 0.34 \text{ (kW)} \times 0.0108 \text{ (h)} \text{ or } 0.00368 \text{ (kWh)}$$

$$\bullet 0.035 \text{ kWh} = 35 \text{ (Wh)}$$

$$\bullet 340 \text{ (W)} \times \frac{13}{1200} \text{ (h)} \text{ or } \frac{221}{60} \text{ (Wh)} \text{ or } 3.683 \text{ (Wh)}$$

Or equivalent e.g W mins

Do not accept incorrect unit.

Do not accept incorrect subject.

**MP2**

Do not allow answers obtained using incorrect

$$\text{power } \left( \frac{126000}{39} \right)$$

$$\text{incorrect power such as } \frac{340}{\frac{126000}{39}}$$

(=) 11% ✓

Accept answer correctly rounded to at least 2 sf.

Calculator display = 10.5238

2

(d) Incorrect:

- this will increase weight **OR** helicopter must provide a greater lift **OR** (more mass therefore) greater GPE (for same height) **OR** (more mass therefore) greater KE (for same speed) **OR** idea that more energy is required. ✓
- the helicopter must displace more (atmospheric) gas (every second to produce greater lift force) **OR** blades must spin faster ✓
- the helicopter must do more work every second (so will transfer stored energy at a greater rate) **OR** the helicopter needs more power to fly ✓

OR

Incorrect:

- this will increase weight ✓
- atmosphere is too thin and can't displace sufficient mass of gas per second **OR** blades can't spin **fast enough** ✓
- can't get off ground due to insufficient lift force ✓

Do not accept increase in resistive forces or increase in drag for increase in weight.

**Must state that it is incorrect for all 3 marks.**

Maximum of 2 marks for suggestions that more than doubles flight time.

Accept lift or thrust or upward force.

A maximum of 1 mark for **MP3** and **MP1** where only mark seen is : idea that more energy is required.

**MP2** can be scored independent of this.

3

- (e) Use of an appropriate equation of motion:

$$v = u + at \checkmark$$

By correct substitution including signs **or** correct rearrangement to make  $t$  subject.

$$(t =) 0.15 \text{ (s)} \checkmark$$

Accept answer correctly rounded to at least 2 sf.

Calculator display = 0.14784946236559

2

- (f) Use of  $v^2 = u^2 + 2as$

**OR**

$$\text{Use of } v = u + at \text{ and } s = ut + \frac{1}{2}at^2 \quad \text{ECF}$$

**OR**

$$mg\Delta h = \frac{1}{2}mv^2 - \frac{1}{2}mu^2 \checkmark$$

$$(h =) 0.61 \text{ (m)} \checkmark \quad \text{ECF}$$

**MP1** (Downward journey)

Allow  $s = 0.65\text{m}$

$$2.2^2 = 0^2 + 2 \times 3.72 \times s$$

**OR**

$$2.2 = 0 + 3.72 t \text{ and } s = 0 + \frac{1}{2} 3.72 t^2 \quad \text{ECF}$$

**OR**

$$m \times 3.72 \Delta h = \frac{1}{2} m 2.2^2$$

**MP1** (Upward journey)

Allow  $s = 0.041 \text{ m}$  obtained from

$$s = 0.55 \times 0.15 - \frac{1}{2} 3.72 \times 0.15^2 \quad \text{ECF}$$

**OR**

$$0^2 = 0.55^2 - 2 \times 3.72 \times s$$

Check possible **ECF** for  $t$  from (e) used in calculation.

Condone sign suppression in **MP1** where answer of 0.65 m or 0.041 m or 0.6(1) m is seen.

Accept answer correctly rounded to at least 2 sf.

Calculator display = 0.60987903225806

2

[15]

**Q15.**

- (a) callipers may **reduce** the (reading of the) diameter ✓  
*treat 'change reading' / 'give incorrect reading' as neutral;*  
*accept the idea that the callipers may 'distort' / 'deform' / 'push in' the putty, eg*  
*'change the shape' / 'crush' / 'squash' / 'cut into' / 'squeeze'*  
*reject implication that density could change, eg*  
*'volume will change' / 'will compress';*  
*reject 'putty will move' / 'not able to grip the putty hard enough'*

1

- (b) average  $d$

OR

uncertainty in  $d$  ✓

percentage uncertainty  $\geq 3$  sf ✓

*answers to >3sf rounding to 2.37(%) earns both marks*

*for ✓ either average = 33.8(0) (mm) OR*  
*uncertainty from half range = 0.8(0) (mm);*  
*allow  $1/2 \times (34.5 - 32.9)$  seen in working;*  
*credit if seen in a percentage uncertainty calculation*

1

percentage uncertainty 2.37(%) ✓

*for ✓ percentage uncertainty to > 3 sf;*  
*reject decimal answer or incorrect rounding to 2.36%;*  
*reject answers if either 32.9 or 34.5 are (wrongly) rejected as anomalous (leading to 1.62% and 1.64% respectively)*

1

- (c) % uncertainty in length correct ✓

*for ✓ minimum 2sf CAO; 2.8(2)%*

1

calculates % uncertainty in volume ✓

*for ✓ % uncertainty in  $V = 2 \times$  their % uncertainty in  $d$  + their % uncertainty in  $L$ ; allow 2.4% for % uncertainty in  $d$*   
*minimum 2 sf; expect 7.6 %*

1

evidence for volume evaluated

OR

evidence for  $\Delta$  volume evaluated  $_{3}\checkmark$

for  $_{3}\checkmark$  accept answers including:

sub of **all data** in to  $V = \frac{\pi \times (\text{theird})^2 \times L}{4}$

OR

sub of **all data** in to

$\Delta V = \frac{\pi \times (\text{theird})^2 \times L}{4} \times \text{their \% uncertainty}$

/  $\Delta V = \text{their volume} \times \text{their \% uncertainty}$

OR

recognisable  $\Delta V$  with POT error

1

$\Delta$  volume between  $4.8$  and  $4.9 \times 10^3 \text{ (mm}^3\text{)}$   $_{4}\checkmark$

answers that round to  $4.8$  or round to  $4.9$  are acceptable;

$_{34}\checkmark$  for  $\Delta$  volume in range and correct POT

1

(d) ruled line  $_{1}\checkmark$

for  $_{1}\checkmark$  line passing below  $5^{\text{th}}$  AND above  $4^{\text{th}}$  ie no overlap between line and either +;

line passing through or extrapolated to  $(0, 0)$  to half a minor grid square;

withhold this mark if line is poorly-marked (if doing so annotate clip to explain)

1

gradient calculated  $_{2}\checkmark$

for  $_{2}\checkmark$  gradient calculated from  $\Delta R$  divided by  $\Delta L^2$ ;

minimum  $\Delta L^2 = 25 (\times 10^{-3} \text{ m}^2)$ ;

allow read-off errors in calculation / allow missing or incorrect POT

1

$\rho$  in range  $3.72$  to  $3.84 (\times 10^{-2})$   $_{3}\checkmark$

for  $_{3}\checkmark$  accept 2 sf  $3.8$

1

POT and unit correct  $_{4}\checkmark$

for  $_{4}\checkmark$  treat  $3.78 \times 10^{-2}$  and  $0.0378 \Omega \text{ m}$  as equally acceptable;

allow alternative valid answer, eg  $37.8 \Omega \text{ mm}$

1

[11]